

**METHOD OF ISOMORPHIC SINGULAR MANIFOLD PROJECTION
STILL/VIDEO IMAGERY COMPRESSION**

Field of the Invention

The present invention relates to image compression systems, and in particular relates to an image compression system which provides hypercompression.

Background of the Invention

5 Image compression reduces the amount of data necessary to represent a digital image by eliminating spatial and/or temporal redundancies in the image information. Compression is necessary in order to efficiently store and transmit still and video image information. Without compression, most applications in which image information is stored and/or transmitted would be rendered impractical or impossible.

10 Generally speaking, there are two types of compression: lossless and lossy. Lossless compression reduces the amount of image data stored and transmitted without any information loss, i.e., without any loss in the quality of the image. Lossy compression reduces the amount of image data stored and transmitted with at least some information loss, i.e., with at least some loss of quality of the image.

15 Lossy compression is performed with a view to meeting a given available storage and/or transmission capacity. In other words, external constraints for a given system may define a limited storage space available for storing the image information,

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or a limited bandwidth (data rate) available for transmitting the image information.

Lossy compression sacrifices image quality in order to fit the image information within the constraints of the given available storage or transmission capacity. It follows that, in any given system, lossy compression would be unnecessary if

5 sufficiently high compression ratios could be achieved, because a sufficiently high compression ratio would enable the image information to fit within the constraints of the given available storage or transmission capacity without information loss.

The vast majority of compression standards in existence today relate to lossy compression. These techniques typically use cosine-type transforms like DCT and
10 wavelet compression, which are specific types of transforms, and have a tendency to lose high frequency information due to limited bandwidth. The "edges" of images typically contain very high frequency components because they have drastic gray level changes, i.e., their dynamic range is very large. Edges also have high resolution. Loss of edge information is undesirable because resolution is lost as well as high
15 frequency information. Furthermore, human cognition of an image is primarily dependent upon edges or contours. If this information is eliminated in the compression process, human ability to recognize the image decreases.

Fractal compression, though better than most, suffers from high transmission bandwidth requirements and slow coding algorithms. Another type of motion (video)
20 image compression technique is the ITU-recommended H.261 standard for videophone/videoconferencing applications. It operates at integer multiples of 64 kbps and its segmentation and model based methodology splits an image into several

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regions of specific shapes, and then the contour and texture parameters representing the region boundaries and approximating the region pixels, respectively, are encoded.

A basic difficulty with the segmentation and model-based approach is low image quality connected with the estimation of parameters in 3-D space in order to impart naturalness to the 3-D image. The shortcomings of this technique are obvious to those who have used videophone/videoconferencing applications with respect particularly to MPEG video compression.

Standard MPEG video compression is accomplished by sending an "I frame" representing motion every fifteen frames regardless of video content. The introduction of I frames asynchronously into the video bitstream in the encoder is wasteful and introduces artifacts because there is no correlation between the I frames and the B and P frames of the video. This procedure results in wasted bandwidth. Particularly, if an I frame has been inserted into B and P frames containing no motion, bandwidth is wasted because the I frame was essentially unnecessary yet, unfortunately, uses up significant bandwidth because of its full content. On the other hand, if no I frame is inserted where there is a lot of motion in the video bitstream, such overwhelming and significant errors and artifacts are created that bandwidth is exceeded. Since the bandwidth is exceeded by the creation of these errors, they will drop off and thereby create the much unwanted blocking effect in the video image. In the desired case, if an I frame is inserted where there is motion (which is where an I frame is desired and necessary) the B and P frames will already be correlated to the new motion sequence and the video image will be satisfactory. This, however,

happens only a portion of the time in standard compression techniques like MPEG. Accordingly, it would be extremely beneficial to insert I frames only where warranted by video content.

The compression rates required in many applications including tactical communications are extremely high as shown in the following example making maximal compression of critical importance. Assuming 512^2 number of pixels, 8-bit gray level, and 30 Hz full-motion video rate, a bandwidth of 60 Mbps is required. To compress data into the required data rate of 128 kbps from such a full video uncompressed bandwidth of 60 Mbps, a 468:1 still image compression rate is required. The situation is even more extreme for VGA full-motion video which requires 221 Mbps and thus a 1726:1 motion video compression rate. Such compression rates, of course, greatly exceed any compression rate achievable by state of the art technology for reasonable PSNR (peak signal to noise ratio) values of approximately 30 dB. For example, the fourth public release of JPEG has only a 30:1 compression rate and the image has many artifacts due to a PSNR of less than 20 dB, while H320 has a 300:1 compression ratio for motion and still contains many still/motion image artifacts.

The situation is even more stringent for *continuity* of communication when degradation of power budget or multi-path errors of wireless media further reduce the allowable data rate to far below 128 kbps. Consequently, state of the art technology is far from providing multi-media parallel channelization and continuity data rates at equal to or lower than 128 kbps.

Very high compression rates, high image quality, and low transmission bandwidth are critical to modern communications, including satellite communications, which require full-motion, high resolution, and the ability to preserve high-quality fidelity of digital image transmission within a small bandwidth communication channel (e.g. T1). Unfortunately, due to the above limitations, state of the art compression techniques are not able to transmit high quality video in real-time on a band-limited communication channel. As a result, it is evident that a compression technique for both still and moving pictures that has a very high compression rate, high image quality, and low transmission bandwidth and a very fast decompression algorithm would be of great benefit. Particularly, a compression technique having the above characteristics and which preserves high frequency components as well as edge resolution would be particularly useful.

In addition to transmission or storage of compressed still or moving images, another area where the state of the art is unsatisfactory is in automatic target recognition (ATR). There are numerous applications, both civilian and military, which require the fast recognition of objects or humans amid significant background noise. Two types of ATR are used for this purpose, soft ATR and hard ATR. Soft ATR is used to recognize general categories of objects such as tanks or planes or humans whereas hard ATR is used to recognize specific types or models of objects within a particular category. Existing methods of both soft and hard ATR are Fourier transform-based. These methods are lacking in that Fourier analysis eliminates desired "soft edge" or contour information which is critical to human cognition.

Improved methods are therefore needed to achieve more accurate recognition of general categories of objects by preserving critical "soft edge" information yet reducing the amount of data used to represent such objects and thereby greatly decrease processing time, increase compression rates, and preserve image quality.

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Summary of the Invention

The present invention is based on Isomorphic Singular Manifold Projection (ISMP) or Catastrophe Manifold Projection (CMP). This method is based on Newtonian polynomial space and characterizes the images to be compressed with singular manifold representations called catastrophes. The singular manifold

10 representations can be represented by polynomials which can be transformed into a few discrete numbers called "datery" (number data that represent the image) that significantly reduce information content. This leads to extremely high compression rates (CR) for both still and moving images while preserving critical information about the objects in the image.

15 In this method, isomorphic mapping is utilized to map between the physical boundary of a 3-D surface and its 2-D plane. A projection can be represented as a normal photometric projection by adding the physical parameters, B (luminance) to generic geometric parameters (X,Y). This projection has a unique 3-D interpretation in the form of a "canonical singular manifold". This manifold can be described by a
20 simple polynomial and therefore compressed into a few discrete numbers resulting in hyper compression. In essence, any image is a highly correlated sequence of data.

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The present invention "kills" this correlation, and image information in the form of a digital continuum of pixels almost disappears. All differences in 2-D "texture" connected with the 2-D projection of a 3-D object are "absorbed" by a contour topology, thus preserving and emphasizing the "sculpture" of the objects in the image.

- 5 This allows expansion with good fidelity of a 2-D projection of a real 3-D object into an abstract (mathematical) 3-D object and is advantageous for both still and video compression and automatic target recognition.

- More particularly, using catastrophe theory, surfaces of objects may be represented in the form of simple polynomials that have single-valued (isomorphic) inverse reconstructions. According to the invention, these polynomials are chosen to represent the surfaces and are then reduced to compact tabulated normal form polynomials which comprise simple numbers, i.e., the datery, which can be represented with very few bits. This enables exceptionally high compression rates because the "sculpture" characteristics of the object are isomorphically represented in the form of simple polynomials having single-valued inverse reconstructions.
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Preservation of the "sculpture" and the soft edges or contours of the object is critical to human cognition of the image for both still and video image viewing and ATR.

- Thus, the compression technique of the present invention provides exact representation of 3-D projection edges and exact representation of all the peculiarities of moving (rotating, etc.) 3-D objects, based on a simple transition between still picture representation to moving pictures.
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In a preferred embodiment the following steps may be followed to compress a still image using isomorphic singular manifold projections and highly compressed data. The first step is to subdivide the original image, I_o , into blocks of pixels, for example 16 x 16 or other sizes. These subdivisions of the image may be fixed in size or variable. The second step is to create a "canonical image" of each block by finding a match between one of fourteen canonical polynomials and the intensity distribution for each block or segment of pixels. The correct polynomial is chosen for each block by using standard merit functions. The third step is to create a model image, I_M , or "sculpture" of the entire image by finding connections between neighboring local blocks or segments of the second step to smooth out intensity (and physical structure to some degree). The fourth step is to recapture and work on the delocalized high frequency content of the image, i.e., the "texture". This is done by a subtraction of the model image, I_M , generated during the third step from the original segmented image, I_o , created during the first step. A preferred embodiment of this entire still image compression process will be discussed in detail below.

Optimal compression of video and other media containing motion may be achieved in accordance with the present invention by inserting I frames based on video content as opposed to at fixed intervals (typically every 15 frames), as in the in prior art motion estimation methods. In accordance with the motion estimation techniques of the present invention, the errors between standard "microblocks" or segments of the current frame and a predicted frame are not only sent to the decoder to reconstruct the current frame, but, in addition, are accumulated and used to

determine the optimal insertion points for I frames based on video content. Where the accumulated error of all the microblocks for the current frame exceeds a predetermined threshold which itself is chosen based upon the type of video (action, documentary, nature, etc.), this indicates that the next subsequent frame after the particular frame having high accumulated error should be an I frame. Consequently, in accordance with the present invention, where the accumulated errors between the microblocks or segments of the current frame and the predicted frame exceed the threshold, the next subsequent frame is sent as an I frame which starts a new motion estimation sequence. Consequently, I frame insertion is content dependent which greatly improves the quality of the compressed video.

The I frames inserted in the above compression technique may first be compressed using standard DCT based compression algorithms or the isomorphic singular manifold projection (ISMP) still image compression technique of the present invention for maximal compression. In either case, the compression techniques used are preferably MPEG compatible.

Additionally, using the motion estimation technique compression of the present invention, compression ratios can be dynamically updated from frame to frame utilizing the accumulated error information. The compression ratio may be changed based on feedback from the receiver and, for instance, where the accumulated errors in motion estimation are high, the compression ratio may be decreased, thereby increasing bandwidth of the signal to be stored. If, on the other hand, the error is

low, the compression ratio can be increased, thereby decreasing bandwidth of the signal to be stored.

Because the present invention is a 3-D non-linear technique that produces high level descriptive image representation using polynomial terms that can be represented by a few discrete numbers or data, it provides much higher image compression than MPEG (greater than 1000:1 versus 100:1 in MPEG), higher frame rate (up to 60 frames/sec versus 30 frames/sec in MPEG), and higher picture quality or peak signal to noise ratio (PSNR greater than 32 dB versus PSNR greater than 23 dB in MPEG). Consequently, the compression technique of the present invention can provide more video channels than MPEG for any given channel bandwidth, video frame rate, and picture quality.

Description of the Drawings

Figure 1A illustrates a singularity called a "fold"; and Figure 1B illustrates a singularity called a "cusp";

Figure 2A illustrates "Newton Diagram Space" and contains "monoms" and polynomials;

Figure 2B illustrates the application of Newton diagram space in the context of ISMP Theory. Canonical and normal forms, etc.;

Figure 3A depicts a fold and Figure 3B depicts tuck;

Figure 4A illustrates a reflection from a manifold;

Figure 4B illustrates the reflection from a manifold depending upon angle θ ;

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Figure 4C illustrates the projection on a display;

Figure 5 illustrates a cylinder with constant luminance dependence;

Figure 6 illustrates an evolvment for $F=X^3$;

Figures 7A and 7B illustrate a reflector of a group for three mirrors R^2 ;

5 Figure 8 illustrates a smooth curve projection, representing movement and a physical object, and a catastrophic frame change, and positionally zoom camera changes;

Figure 9 is a abbreviated flow chart of the inventive ISMP still image compression method;

10 Figure 10 is a detailed flow chart of the inventive ISMP compression method in accordance with the present invention;

Figure 11A illustrates an original image with an enlarged edge contour;

Figure 11B shows a 2-D CCD image of the enlarged edge contour;

15 Figure 11C illustrates a model surface of the original edge contour in accordance with the present invention;

Figure 12 is an illustration of a segment of an original frame in accordance with the present invention;

Figure ^{13A-13C} ~~13~~ is an illustration of connecting segments of a frame in accordance with the present invention;

20 Figure ^{14A-14C} ~~14~~ illustrates subtracting I_M from I_O in accordance with the present invention;

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Figure 15 is a flow chart of the decoding process for ISMP compression in accordance with the present invention;

Figure 16 is a flow chart of the motion estimation process in accordance with the present invention;

5 Figure 17 is a circuit schematic of the hardware ^{used} [uses] for motion estimation in accordance with the present invention;

Figure 18 is a flow chart of the error accumulation method of the present invention; and

10 Figure 19 is a table showing the results of data communication with varying data rates in accordance with the present invention.

Description of the Preferred Embodiments

Preliminary Discussion of the Mapping of Surfaces Using Catastrophe Theory

The following is a brief introduction to Catastrophe Theory which may be helpful in understanding novel compression methodology of the present invention.

15 Further discussion may be found in B.I. Arnold, *Catastrophe Theory*, Springer-Verlag 1992, which is incorporated by reference herein.

Catastrophes are abrupt changes arising as a sudden response of a system to a smooth change in external conditions. In order to understand catastrophe theory, it is necessary to understand Whitney's singularity theory. A mapping of a surface onto a
20 plane associates to each point of the surface a point of the plane. If a point on the surface is given coordinates (x_1, x_2) on the surface, and a point on the plane is given

coordinates (y_1, y_2) , then the mapping is given by a pair of functions $y_1 = f_1(x_1, x_2)$ and $y_2 = f_2(x_1, x_2)$. The mapping is said to be *smooth* if these functions are smooth (i.e., are differentiable a sufficient number of times, such as polynomials for example). Mappings of smooth surfaces onto a plane exist everywhere. Indeed, the majority of objects surrounding us are bounded by smooth surfaces. The visible contours of bodies are the projections of their bounding surfaces onto the retina of the eye. By examining the objects surrounding us, for instance, people's faces, the singularities of visible contours can be studied. Whitney observed that generically (for all cases bar some exceptional ones) only two kinds of singularities are encountered. All other singularities disintegrate under small movements of the body or of the direction of projection, while these two types are stable and persist after small deformations of the mapping.

An example of the first kind of singularity, which Whitney called a fold, is the singularity arising at equatorial points when a sphere is projected onto a plane such as shown in Figure 1A. In suitable coordinates, this mapping is given by the formulas

$$y_1 = x_1^2, \quad y_2 = x_2$$

The projections of surfaces of smooth bodies onto the retina have just such a singularity at generic points, and there is nothing surprising about this. What is surprising is that besides the singularity, the fold, we encounter everywhere just one other singularity, but it is practically never noticed.

The second singularity was named the *cusp* by Whitney, and it arises when a surface like that in Figure 1B is projected onto a plane. This surface is given by the equation

$$y_1 = x_1^3 + x_1 x_2, \quad y_2 = x_2$$

with respect to spatial coordinates (x_1, x_2, y_1) and projects onto the horizontal plane (x_2, y_1) .

On the horizontal projection plane, one sees a semicubic parabola with a cusp (spike) at the origin. This curve divides the horizontal plane into two parts: a smaller and a larger one. The points of the smaller part have three inverse images (three points of the surface project onto them), points of the larger part only one, and points on the curve, two. On approaching the curve from the smaller part, two of the inverse images (out of three) merge together and disappear (here the singularity is a fold), and on approaching the cusp all three inverse images coalesce.

Whitney proved that the cusp is *stable*, i.e., every nearby mapping has a similar singularity at an appropriate nearby point (that is, a singularity such that the deformed mapping, in suitable coordinates in a neighborhood of the point mentioned, is described by the same formulas as those describing the original mapping in a neighborhood of the original points). Whitney also proved that every singularity of a smooth mapping of a surface onto a plane, after an appropriate small perturbation, splits into folds and cusps. Thus, the visible contours of generic smooth bodies have cusps at points where the projections have cusp singularities, and they have no other

where, their singularities must be of
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ce. This [simple] idea is the whole

Abstract

Technical Foundation of Catastrophic Theory

Catastrophic Manifold Projection (CMP) or Isomorphic Singular

Manifold Projection (ISMP)

The following glossary is a useful aid to understanding catastrophe theory because

5 many of the terms used to describe it are uncommon in mathematics.

- **2-D Cartesian (Plane) Coordinates** refer to standard (u, v) coordinates that describe a plane projection.

- **2-D Generalized Coordinates:** (ξ, ν) describe a system through a minimum number of geometrical coordinates (i.e., a number of degrees of freedom). These are usually curvilinear local coordinates, which
10 belong to a specific surface in the vicinity of some point (i.e., origin of coordinates).

- **3-D Cartesian Coordinates** refer to (x, y, z) describing a common surface in 3-D: $F(x, y, z) = 0$.

- **3-D Cartesian (Hyperplane) Coordinates**, are: (u, v, w) , where
15 (u, v) are 2-D (plane) Cartesian coordinates; w is a third, new physical coordinate, related to luminance (B) and describing a "gray level" scale color scale.

- **Arnold (Vladimir)** is a Russian mathematician, who is a major
20 contributor to catastrophe theory.

- **Arnold Theorem (Local Isomorphism)** A family of transformations can transform any given mapping into a set of canonical

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transformations by using smooth substitutions of coordinates. The Arnold theorem defines local isomorphism in a sense that defines a class of locally isomorphic functions.

- 5 1. Arnold proved that Thom's theory can be represented in terms of group theory. 2. He also introduced an elegant theory for construction of the canonical form of singularities as they apply to wave front propagation in Lagrangian mechanics. 3. Furthermore, Arnold introduced methods based on using algebra of vector fields

$$v = \sum_i R_i \frac{\partial}{\partial x_i} ,$$

- 10 where R_i is a polynomial.

- and introduced a method of *spectral series* for reduction of arbitrary functions to normal form. 4. Finally, he introduced classification of singularities and a method that described how to determine any type of singularity within a list of singularities.
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- **Canonical Form** is a generic mathematical term that can be defined in various ways. In the specific context of the Arnold theorem, the *canonical form* is the simplest polynomial, with the highest degree of monoms within the normal form area, representing a given type of

catastrophe. The *canonical form* is represented by a segmented line in a Newton diagram.

- 5 • **Canonical Transformation** permits transformation of real surface form (such as $F(u, v, w) = 0$) into canonical form (i.e., superposition of Morse form and singular residuum, or Thom form) into two blocks of so-called canonical coordinates: regular and catastrophic.
- 10 • **Catastrophe** (a term invented by Montel) is a specific manifold mapping feature by which some points lying in the projection plane can abruptly change location in manifold. More philosophically, it "describes the emergence of discrete structures from the typical surface described in the platform of continuum."
- 15 • **Catastrophes, Critical Number** in 3-D (for mapping a generic surface onto a plane) is only two (2): *fold* and *cusp (tuck)*. Using these two catastrophes is sufficient for static still imagery.
- 20 • **Catastrophes, Total Number** in 3-D (for mapping a generic surface onto a plane) is fourteen (14). Only "fold"-catastrophe does not have degenerate points; all the (13) others have. Using all 14 catastrophes is necessary in hypercompression if we consider dynamic imagery (or video).
- **Catastrophic Manifold Projection** is a fundamental concept of "3-D into 3-D" mapping, leading to *hypercompression*. This is

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diffeomorphic mapping, including geometrical coordinates (2-D generalized, and 2-D plane), as well as a fourth "photometric coordinate".

- **Catastrophic Manifold Projection (CMP) Law** is mapping:

$$(\xi, \nu, B) \Leftrightarrow (u, \nu, w)$$

Thus, the CMP is "3-D into 3-D" mapping, with two types of coordinates:

5 "geometrical" $(\xi, \nu); (u, \nu)$, and "photometric" (B, w) .

- **The Critical Point** is a point at which the rank of Jacobian is less than maximal (examples are maxima, minima, and bending points)

10 • **Datery** result from a novel mathematical procedure leading to a tremendous compression ratio; instead of describing some surface by a continuum, we describe this singular manifold by a few low even numbers, i.e., datery. Therefore, during *hypercompression*, the surface as continuum "disappears", leaving typical data (such as computer data).

15 • **In a Degenerate Critical Point**, the rank of Jacobian is a less than maximal rank minus one. This point can be a critical point of *cusp* catastrophes, for example.

- **Discrete Structures** are singular manifolds that can be described by a set of discrete, usually even, data (e.g., $(2, 5, -1, 3)$), leading to *datery* instead of description by a continuum of points (such as $F(x, y, z) = 0$). Such discrete structures (which are, in fact, continuums, but are still

described by discrete sets), are typically referred to as *singularities*, *bifurcation*, or *catastrophes*.

- **Diffeomorphism** is a stronger term than isomorphism (or homeomorphism), and means not only isomorphism, but also smooth mapping.

- **Discrete Structures** are singular manifolds that can be described by a set of discrete data (e.g., $(2,5,-1,3)$), leading to *datery*, instead of description by continuum of points (such as $F(x,y,z) = 0$). These discrete structures (which are, in fact, continuums, but are still described by discrete sets), are typically referred to as *singularities*, *bifurcation*, or *catastrophes*.

- **Field**, a subset of a *ring*. (All non-zero *field* elements generate a *group*, by multiplication.) For example, the differential operator can be an element of a field.

- **Generalized Coordinates**, or, more precisely, generalized coordinates of Lagrange, are such "natural" coordinates in solid state mechanics that their number is precisely equal to the number of a body's degrees of freedom: (ξ, ν, η, \dots)

- **A Generic Surface**, in the context of the CMP method, is a mathematical surface which, within infinitesimal changes, does not have the same tangent (or projection line) for more than two points along any curve lying on this surface. In other words, a surface is generic if small

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changes to the surface do not lead to changes in singularities (such as splitting into less complex ones.) Physical surfaces are almost always *generic* because of noise tolerance.

5 • A **Group** is the simplest set in *mathematical models*, with only a single operation.

• **Hypercompression** is a specific compression term which provides a *datery* (i.e., "stripping" a continuum surface into its discrete representation). This is possible for the surface locality in the form of catastrophe.

10 • **Ideal** is another subset of a ring. A subset of the ring is an ideal if this subset is a subgroup of the ring by summation. In the context of the Arnold theorem, this summation group is a set of all *monoms* that lie above the canonical form segmented line.

• **Isomorphic Singular Manifold Projection** - see CMP.

15 • **Jacobian** is a transformation matrix whose element, H_{ij} , can be presented in the form:

$$H_{ij} = \frac{\partial u_i}{\partial \xi_j}$$

where $u_i = (u, v, w)$ is the plane projection Cartesian coordinate system, $\xi_j = (\xi, \nu, \eta)$ is the generalized coordinate system, and

$$\frac{\partial u}{\partial \xi}$$

describes a partial derivative.

- **Landau (Lev)** was a Russian theoretical physicist, who won the Nobel Prize for superfluidity of the isotope helium He_3 . He systematically applied the catastrophe theory approach before this theory was mathematically formulated [3].

- The **Landau Method**, applied in the second-order phase transition, applies Thom's lemma in the form of the Taylor series, including only "important" physical terms.

- **Lie Algebra** is an algebra belonging to the *Lie groups* with a binary operation (commutator).

- A **Lie Group** is a group whose generator is an infinitesimal operator.

- **Locally Isomorphic** functions have the same singular residuum (see Thom's lemma); thus, they can be compressed identically for "soft edges", or "object boundaries".

- **Manifold** is a mathematical surface (curve or point) defined locally by a system of equations through local "*canonical*" coordinates, also called curvilinear (natural) coordinates, or *generalized coordinates* of Lagrange (known as *generalized coordinates* for short).

- **Mapping** is a transformation in which

$$v = g(\xi, \nu)$$

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- A **Newton Diagram** is discrete (Cartesian) 2-D "point" space defined in such a way that the x-axis and the y-axis describe x-polynomial and y-polynomial power, respectively. For example, the x^2y -polynomial element is equivalent to point (2,1) in Newton table space. In this *Newton diagram* space, a given polynomial that is always normalized (i.e., with

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- **Thom's lemma** is a fundamental theorem of catastrophe theory in general and the ISMP in particular, as a generalization of the Morse lemma for degenerate critical points. It claims that, in such a case, the algebraic form describing a surface can no longer be only quadratic, but

consists of a quadratic form (as in the Morse lemma) and an additive singular residuum:

$$f = \sum_{i=1}^s k_i \alpha_i^2 + g(\alpha_{s+1}, \dots, \alpha_n), \quad k_i = \pm 1$$

These normalized coordinates are also separated into two parts: *non-generate point coordinates* (NPC) ($i = 1, 2, \dots, s$) and *degenerate point coordinates* (DPC) ($i = s+1, s+2, \dots, n$). In the residuum function $g(\alpha_{s+1}, \dots, \alpha_n)$, the first- and second-order differentials vanish: $dg = d^2g = 0$. Functions with the same g belong to a set of stable equivalent functions, or are *locally isomorphic* (Arnold).

- The **Thom Statement** declares that there is a finite number of catastrophes (14) in 3-D space.
- 10 • A **Vector Field** is a representation whose element provides a shift of polynomials in the Newton diagram (this shift does not need to be a translation).
- **Whitney (M.) (1955)** was an American mathematician, and a major contributor to catastrophe theory. His major achievements were in
- 15 studying mapping from surface to plane.
- **Whitney Theorem (Two Stable Catastrophes):** The local normal form of the singularities of typical stable mappings from 2-D manifolds (in 3-D) to a plane can be either fold or cusp only. (**Stable Mapping**): Every singularity of smooth mapping of a surface onto a plane after an

appropriate small perturbation splits into stable catastrophes only (fold and cusp). This theorem is applied in CMP hypercompression into still imagery.

The following references are referred to in the text that follows and are hereby
5 incorporated by reference.

1. M. Born, E. Wolf, *Principles of Optics*, Pergamon Press, 1980.
2. T. Jansson, "Radiance Transfer Function," J. Opt. Soc. Am. Vol. 70, No. 12,
1980] pp. 1544-1549.
3. V.I. Arnold, *Catastrophe Theory* Springer-Verlag, NY, 1992.
- 10 4. V.I. Arnold, *Singularities of Caustics and Wave Fronts, Mathematics and Its Applications* (Sovien Series) Vol. 62, Kluwer Academic Publisher, 1990.
5. V.I. Arnold, *The Theory of Singularity and its Applications*, Academia Nazionale dei Lincei, 1993.
6. V.I. Arnold, S.M. Gusein-Zade, A.N. Varchenko, *Singularities of Differential*
15 *Mapping*, Birkhäuser, Boston-Basel-Berlin, 1988.
7. R. Gilmore, *Catastrophe Theory for Scientists and Engineers*, John Wiley & Sons, New York, 1981.
8. P. Grey, *Psychology*, Worth Publishers, New York, NY, 1991.

The following are expanded definitions, theorems, and lemmas referred to in the
20 discussion below:

Critical Point: For a function depending on n variables ($\xi \in \mathbb{R}^n$ or n -dimensional magnified), a critical point is called nondegenerate if its second differential is a nondegenerate quadratic form. In other words, for this point, only one row of the Jacobian is equal to zero.

- 5 **Noncritical Point:** In the neighborhood of *regular* (or noncritical) point transformations of n local coordinates ξ_i of a surface into coordinates u_i on a mapping plane, the transformation can be written as:

$$u_i = u_i(\xi_1, \dots, \xi_n), \quad i = 1, \dots, n.$$

- In this case, the *Jacobian* is always nondegenerate. This means that in the vicinity of
10 this point, it is possible to do an isomorphical transformation according to the implicit function theorem:

$$\xi_i = \xi_i(u_1, \dots, u_n), \quad i = 1, \dots, n$$

Morse lemma: In the neighborhood of a nondegenerate critical point, a function may be reduced to its quadratic part, i.e., it may be written into the normal form

$$u = \xi_1^2 - \dots - \xi_k^2 + \xi_{k+1}^2 + \dots + \xi_n^2 \quad (1)$$

- 15 for a certain local coordinate system (ξ_1, \dots, ξ_n) .

The meaning of this lemma is as follows: Since the *Jacobian* of any smooth function f is nonzero in the vicinity of any nondegenerate critical point, differential replacements, such as:

$$u_i = u_i(\xi_1, \dots, \xi_n) \quad (2)$$

can transform this function into a nondegenerate quadratic form:

$$u_i = \sum_{i=1}^n k_i \xi_i \quad k = \pm \quad (3)$$

At a degenerate critical point, some eigenvalues of the Jacobian matrix are zero. The subspace spanned by the corresponding eigenvalues $(\xi_{s+1}, \dots, \xi_n)$ is a critical subspace and has a dimension equal to the co-rank of the critical point.

- 5 Function f can be written in the form defining **Thom's lemma**, which is fundamental to the ISMP:

$$u_j = \sum_{i=1}^s k_i \xi_i^2 + g(\xi_{s+1}, \dots, \xi_n) \quad k_i = \pm 1 \quad (4)$$

where $g(\xi_{s+1}, \dots, \xi_n)$ is a function (residuum) for which $dg = d^2g = 0$.

All functions with the same g are called a differential equivalent. The term local isomorphical is used as another description of that class of function.

- 10 Thom's lemma provides a basis for an application mapping algorithm for any surfaces that can be mapped on an image plane.

Thom's form can be used as a nondegenerate function for image approximation, but using singularities analysis allows extraction of the most important information from an image.

- 15 **1st Whitney Theorem.** The local normal form of the singularities of typical mappings from two-dimensional manifolds to a plane (or to another two-dimensional manifold):

$$cusp \begin{cases} \mu = \xi^3 + \xi\eta \\ \nu = \eta \end{cases} \quad (5A)$$

$$fold \begin{cases} u = \xi^2 \\ v = \eta \end{cases} \quad (5B)$$

$$regular \begin{cases} u = \xi \\ v = \eta \end{cases} \quad (5C)$$

Stable catastrophes (fold and cusp) are sufficient for still image compression. Fig. 3A depicts a fold and Figure 3B depicts a cusp.

2nd Whitney Theorem: *Every singularity of a smooth mapping of a surface onto a plane after an appropriate small perturbation splits into folds and cusps.*

5 **Arnold Theorem:** There is a family of transformations that can transform any
 given mapping into a set of *canonical* transformations by using smooth substitution.

$$\begin{aligned} & (\xi, \eta) \rightarrow (u, v) \\ & u = u(\xi, \eta) \\ & v = v(\xi, \eta) \end{aligned} \quad (6)$$

10 then, by using smooth diffeomorphic transformation into new "plane" coordinates (u' ,
 v'), we obtain:

$$\begin{aligned} u' &= a_1 u + a_2 v + a_3 u^2 + \dots \\ v' &= b_1 v + b_2 u + b_3 v^2 + \dots \end{aligned} \quad (7A)$$

$$\begin{aligned} u'' &= c_1 u' + c_2 v' + c_3 u'^2 + \dots \\ v'' &= d_1 v' + d_2 u' + d_3 v'^2 + \dots \end{aligned} \quad (7B)$$

We can obtain

$$u = M_1 (\xi'', \eta'') + F_{C1} (\xi'', \eta'') + F_{C2} (\xi'', \eta'') + \dots \quad (8)$$

$$v = M_2 (\xi'', \eta'') + F_{C3} (\xi'', \eta'') + \dots$$

- 5 where M_1 and M_2 are Morse forms and F_{C1} , F_{C2} , F_{C3} , ... are canonical (singular) forms.

- In the Arnold theorem, Thom's lemma is applied in such a sense that we represent a Thom form (as in Eq. 8) by superposition of Morse (smooth) forms (M), and Thom residual forms (F_C). The proof of this theorem is based on *spectral series* reduction to normal forms. This is a *local isomorphism* (or, more precisely, *local diffeomorphism*),
- 10 because each catastrophe is represented by a given *canonical form*, which, in turn, generates a *normal form*. Moreover, each catastrophe is represented by only one *canonical form*. Therefore, while general mapping is usually not isomorphic, in this specific case, *Arnold mapping* is. The consequence of the Arnold theorem, proven by his students Platonova and Shcherback, is a statement made earlier by Thom:
- 15 *The number of nonequivalent singularities in the projections of generic surfaces in 3-D space, defined by the families of rays issuing from different points of space outside the surface, is finite and equal to 14.*

Physical Modeling by Catastrophic Manifold Projection

Smooth surfaces vs. image presentation

Usually, 3-D objects, presented in the form of 2-D images, are projections of the following types of objects:

- 5 1. **Smooth artificial and natural objects:** This category can be described as a projection of idealized surfaces on the image plane. In accordance with the human visual system, we first try to extract objects that can be presented by smooth surfaces ("soft edges").
- 10 **Edges of smooth surfaces:** These soft edges, which appear during mapping, are the same as the visible contours of smooth objects. (These objects ideally fit into the proposed approach.)
- 15 2. **Sharp joints of objects:** One example is the corners of buildings. (These jumps can also be naturally described by the proposed approach.)
3. **Textures of an object:** These objects will be described by the proposed method with natural scale parameters (including fractal type textures).

00123456789101112131415161718192021222324252627282930313233343536373839404142434445464748495051525354555657585960616263646566676869707172737475767778798081828384858687888990919293949596979899

Physical Model Formulation

Formation of an image can be described as light reflection from a general surface. It may be an actual radiation surface (light source, transparent surface, or semi-transparent surface) or it may be an opaque reflected surface. We have introduced a
 5 *photometric projection*, so each ray is reflected backward only, in accordance with the radiance projection theorem ^[2]. The reflection is the highest in the specular direction, and it is monotonically reduced, with an increase of the reflection direction separation from the specular direction, as shown in Figure 4. This *photometric projection* approach can be derived from Thom's lemma and the Arnold theorem.

10 If a reflection is identified with reflection surface luminance, B , the dependence of B on the direction will depend on the nature of the surface (whether it is smooth or rough). There is no general theory for arbitrary surfaces, although there are two limited cases: *Lambert's cosine law*, in which B is a constant (isotropic case), and the specular (mirror) reflection, in which incident light is reflected, without distortion, only in the
 15 specular direction. In a general case, we have intermediate distribution as seen in Figure 4A which is a reflection from a manifold, 4B which is an explanation of reflection value depending upon angle θ , and 4C which is what would be displayed, for example, on a display. The presented photometric projection has a natural interpretation: the reflection value decreases when the θ -value increases, and vice versa.

Catastrophic Manifold Projection (CMP)

Inverse projection from a 2-D plane into the surface of a real object is analyzed. The geometry of this problem (i.e., *photometric projection*) has been shown in Figure 4. Now, however, this inverse problem must be formulated in precise mathematical terms, allowing design of a suitable algorithm for hypercompression. To do this, the *forward* problem of image formation is formulated first.

In general, image formation can be presented as differential mapping from 4-D space (x, y, z, B) ; where x, y, z are real 3-D space coordinates of a point and B is the luminance of that point) to the image plane (u, v, w) , where u and v are coordinates of a pixel and w is a color (or gray scale level) of the pixel. The result of mapping the manifold with internal curvilinear (ξ, η) coordinates will be a 3-D surface (u, v, w) ; where u, v are coordinates of the point into the plane and w is the luminance of the point.

The mapping will be:

$$u = f_1(x, y, z) \quad (9A)$$

$$v = f_2(x, y, z) \quad (9B)$$

$$w = f_3(x, y, z, B). \quad (9C)$$

or

$$u = F_1(\xi, \eta) \quad (10A)$$

$$v = F_2(\xi, \eta) \quad (10B)$$

$$w = F_3(\xi, \eta, B) \quad (10C)$$

where f_1 and f_2 are regular projections of a surface to a plane, f_3 is luminance projection, and F_1, F_2, F_3 are their equivalents in the curvilinear coordinate system (ξ, η) .

To formulate the isomorphic singular manifold projection (ISMP) problems by applying Thom's lemma formalism (i.e., canonical form, catastrophes, etc.), one must realize first that the $w(B)$ - dependence is a smooth monotonic one, since both w and B are various forms of luminance, in such a sense that B is the physical luminance, while w is its representation in the form of color (gray level) in the CCD plane. But, smooth dependence does not contain critical points (even nondegenerate ones). Therefore, Thom's (splitting) lemma can be applied to Function (10), in the form:

$$w = M(B, \xi, \eta), \quad \text{or} \quad (11A)$$

$$w = M(B, \xi) + g(\eta), \quad \text{or} \quad (11B)$$

$$w = M(B, \eta) + g(\xi), \quad \text{or} \quad (11C)$$

$$w = M(B) + g(\xi, \eta), \quad (11D)$$

where the first function M represents a monotonical function of B or (function without critical points), and $g(\xi, \eta)$ represents all singularities of projection influencing a gray scale level (color) of a given point (i.e., g -function represents a singular Thom residuum).

In order to show this, Function (10C) is expanded into infinite Taylor series, in the vicinity of ξ_0, η_0 , and B_0 , in the form:

$$\begin{aligned}
w = w_0 &+ \frac{1}{1!} \frac{\partial F_3}{\partial \xi} \Big|_{\xi_0} (\xi - \xi_0) + \frac{1}{1!} \frac{\partial F_3}{\partial \eta} \Big|_{\eta_0} (\eta - \eta_0) + \frac{1}{1!} \frac{\partial F_3}{\partial B} \Big|_{B_0} (B - B_0) \\
&+ \frac{1}{2!} \frac{\partial^2 F_3}{\partial \xi^2} \Big|_{\xi_0} (\xi - \xi_0)^2 + \frac{1}{2!} \frac{\partial^2 F_3}{\partial \eta^2} \Big|_{\eta_0} (\eta - \eta_0)^2 + \frac{1}{2!} \frac{\partial^2 F_3}{\partial B^2} \Big|_{B_0} (B - B_0)^2 \quad (12) \\
&+ \frac{1}{2!} \frac{\partial^2 F_3}{\partial \xi \partial B} \Big|_{\xi_0 B_0} (\xi - \xi_0)(B - B_0) + \frac{1}{2!} \frac{\partial^2 F_3}{\partial \eta \partial B} \Big|_{\eta_0 B_0} (\eta - \eta_0)(B - B_0) + \dots
\end{aligned}$$

It should be noted that neither linear form of this Taylor series can be singular, by definition, and, therefore, neither is of interest. In relation to quadratic terms, coordinate substitution will be provided so that after this substitution, some free coefficients will be received that permit the zeroing of mixed quadratic terms (this approach is completely within the framework of Thom's lemma proof). On the other hand, the quadratic term $(B-B_0)^2$ is a Morse term. Therefore, it is demonstrated that there are no singular B-dependent terms. In summary, a luminance physical coordinate does not introduce new singularities, and, because g depends only on geometrical coordinates (ξ, η) (belonging to 3-D space manifold), all previous results of the Whitney-Thom-Arnold theory apply in this new geometrical/physical ("geophysical") 4-D space. (See Table 1.)

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Table 1

Type of singularity	Name of singularity	Formula	Singularity Applications
0	Regular	$u = \xi$ $v = \eta$	Areas located on still image plane.
1	Fold	$u = \xi^2$ $v = \eta$	Lines located on still image planes (contours of objects).
2	Cusp (Tuck)	$u = \xi^3 + \xi\eta$ $v = \eta$	Points located on still image plane (with transitions to folds and regular point). Critical points necessary for recognizing images (such as corner of mouth, eyes, etc.).
3-14	Other	Not presented here due to complexity and lack of space. See Ref [3].	Special directions of mappings for still images. Points of movie frames necessary for recognizing a motion (e.g., two-humped camel rotation).

In order to explain these new results, a simple example of a homogeneous object with constant luminance B is considered.

Example 1: Arbitrary object with constant luminance

In such a case, Eq. (10C) does not contain B-dependence; i.e., it can be written in the following form:

$$w = F_3(\xi, \eta) \quad (13)$$

Now, the first two equations (10A) and (10B) can be used without changes, to introduce (u, v) - coordinates, in the form:

$$w = F(u(\xi, \eta), v(\xi, \eta)) \quad (14)$$

where F is some new function, and

$$w = F_3(\xi, \eta). \quad (15)$$

It is clear that w -coordinate should have the same singularities as u and v (see Table 1).

In this case, all changes in color (gray level) will be determined only by mapping F and the contour of an object. Of course, the singularities for color w will be located at the same points as singularities of u and v . As a consequence, the singularities of color will be displaced at the contour of the object.

Example 2: Cylinder with given luminance dependence

Mapping of a cylinder with a given constant luminance dependence is shown in Figure 5 and described as follows:

$$B = f(\xi, \eta). \quad (16)$$

In a cylindrical coordinate system (where axis y coincides with the axis of the cylinder), $x = \alpha$, where α is angle $\angle BOA$, and z is distance OB (or, radius).

Two parametric coordinates, $\xi = \alpha$, where α is angle $\angle BOA$ (A is the central point of cylinder, B is a given point); y is the axial coordinate, and $z (=R$, where R is const) is the radius vector (OB). That the w -parameter must be proportional to B , everywhere must be taken into account. This means that B does not create any singularities. For new coordinates on the image plane:

$$u = R \sin(\xi) \quad (17A)$$

$$v = \eta \quad (17B)$$

$$w = C \cdot B + f(\xi, \eta); \quad C = \text{const} \neq 0. \quad (17C)$$

On the other hand, a geometrical analysis of transformation Eq. (9A) shows that y - does not produce any singularities (since y is an axial coordinate). Therefore, it can be assumed, without loss of generality, that w depends only on x and B in the following form:

$$5 \quad w = C \cdot B + f(u(\xi)) \quad (18)$$

or

$$w = C \cdot B + f'(x) \quad (19)$$

where $f'(x) = f(u(x))$.

For critical point estimation, the Jacobian is considered, transforming
10 coordinates (ξ, η, B) into (u, v, w) in the form:

$$H_{ij} = \begin{bmatrix} \frac{\partial u}{\partial x} & \frac{\partial u}{\partial y} & \frac{\partial u}{\partial z} \\ \frac{\partial v}{\partial x} & \frac{\partial v}{\partial y} & \frac{\partial v}{\partial z} \\ \frac{\partial w}{\partial x} & \frac{\partial w}{\partial y} & \frac{\partial w}{\partial z} \end{bmatrix} = \begin{bmatrix} R \cos(x) & 0 & 0 \\ 0 & 1 & 0 \\ C \frac{\partial B}{\partial u} \frac{\partial u}{\partial x} + \frac{\partial f}{\partial u} \frac{\partial u}{\partial x} & 0 & C \end{bmatrix} \quad (20)$$

or

$$h_{ij} = \begin{bmatrix} R \cos x & 0 & 0 \\ 0 & 1 & 0 \\ \left(C \frac{\partial B}{\partial u} + \frac{\partial f}{\partial u} \right) R \cdot \cos(x) & 0 & C \end{bmatrix}$$

The first row of the matrix is not equal to 0, except

$$x = \pm \frac{\pi}{2}$$

Therefore, it is possible to use a smooth transformation between (x, y, z) and (u, v, w) .

$$(\xi, B) \Rightarrow (u, w) \quad (21)$$

and there are no singularities for

$$|x| \neq \frac{\pi}{2}$$

but if

$$x = \pm \frac{\pi}{2}$$

the first row becomes 0 and the determinant equals 0. This means that in the case of

$$x = \pm \frac{\pi}{2}$$

we cannot perform smooth variable substitution, and singularities exist in these points

5 (projection of *fold*).

Let function w be represented in the expanded Taylor series:

$$w(\xi, B) = CB + f(\xi_0, B_0) + \frac{\partial f}{\partial u} \cdot \frac{\partial u}{\partial \xi} (\xi - \xi_0) + \dots \quad (22)$$

The significance of a nondegenerate point

$$x = \pm \frac{\pi}{2}$$

(fold) becomes clear if it is realized that even in the case of v , a weak dependence

between w and x ,

$$\frac{\partial u}{\partial x}$$

grows to infinity (in the vicinity of

$$x = \pm \frac{\pi}{2}).$$

Because the singularity appears as a result of geometrical mapping (not connected to changes of color), and we assume that the color of an object is a smooth function of coordinates x_1, x_2 , it is possible to use a *canonical function* for representation of function f' :

$$f'(x_1, x_2) = Bx_3 + c \cdot F(x_1)$$

where F is the deformation ^[3] of a canonical polynomial (fold or $x^{1/2}$ type dependence).

The calculations presented above do not use rigorous mathematical calculations, but they are very close to *Lev Landau's approach*, applied successfully to many areas of theoretical physics. In his approach, the art of throwing away "inessential" terms of the Taylor series, and preserving smaller size, yet "physically important" terms, has been rigorously proven through the course of the catastrophe theory ^[3].

Drawbacks of Fourier Analysis

Describing an arbitrary function by using a standard transform, such as *Fourier* or *wavelet*, is natural for periodic signal analysis. In image processing, however, these approaches have difficulties with describing very high redundancy regions with flat, slow-changing parts, as well as regions of abrupt change (or "soft edges"). Such classical description is unnatural for these types of objects because it

At the same time, starting from Leibniz, Huygens, and Newton, a clear

5 and surfaces. As discovered recently, this approach has become strongly related to

of the unique properties of this approach, consider the classic evolver problem,

10 For example, for $f=x^3$, the evolvent presented in Figure 6 can be constructed.

If complex space C^3 instead of R^3 is analyzed, the factor-space of C^3 for this

invariants. By using these invariants, any polynomials of this group can be

simplified example of three mirrors on \mathbb{R}^2 as seen in Figs 7A and 7B.

20 4A) belong to one (regular) orbit. Points located on the mirrors belong to another

orbit. A set of all irregular orbits in a factor space is a discriminant (i.e., the manifold in a factor space).

Now the plane in 3-D space can be represented, as in Figure 4, as a plane with coordinates z_1, z_2, z_3 . The plane can be determined by:

$$z_1 + z_2 + z_3 = 0 \quad (23)$$

In this space, it is possible to introduce permutation of the axis, generated by reflections.

5
$$z_i = z_j \quad (24)$$

Orbits in this context constitute a set of numbers $\{z_1, z_2, z_3\}$ (with all permutations generated by reflections), with the additional condition of Eq. (23).

This unordered set will be uniquely determined by polynomials:

$$z^3 + \lambda_1 z^2 + \lambda_2 z + \lambda_3 = 0 \quad (25)$$

By using Eq. (25), the following is obtained:

$$\lambda_1 = 0$$

10 or

$$z^3 + az + b = 0 \quad (26)$$

The space of the orbits of this group will be naturally presented by the roots of a cubic polynomial Eq. (26). This means that in factor space, this space is just a plane with coordinating (a, b) .

15 Each point (a, b) of this space corresponds to a cubic polynomial and its roots.

If some of the roots are equal, that means we have received irregular orbits.

The discriminant in this case is

$$4a^3 + 27b^2 = 0 \quad (27)$$

which is of $3/2$ type curve. This curve corresponds to specific orbits (in the mirrors) in Figure 4A.

For all other types of groups generated by reflection, analogical construction of the discriminant exists.

- 5 It can be proven (Arnold; see Ref. [6]) that the surface creating the evolvent is diffeomorphical to the discriminant of the H_3 icosahedron group. As a result, by using the group representation, the redundancy of a mathematical object that is diffeomorphical to our mapping procedure has been greatly reduced.

- 10 Taking into account the symmetry of 3-D objects mapping (symmetry in a general sense, this means the Lie group, in this case) can optimally reduce redundancy and extract the information that describes the most important features of our object.

- 15 In summary, the polynomial representation of geometrical objects (starting from: *Newton* through *Bernoulli*, up to *Thom* and *Arnold*) seems to be more natural than the common *Fourier* (and *wavelet*) approach, because polynomials are connected to groups of symmetry that permit reduction in orbit redundancy in a most natural way.

Catastrophe Theory Applied to Still Image Compression

- 20 Because the most critical part of an object -- its 3-D *boundary* -- can be described by a 1-D contour and three or four natural digits or "coefficients" that characterize a simple catastrophic polynomial, tremendous lossless compression of object boundaries can be achieved, far exceeding state of the art compression ratios while still preserving high quality image. Since in all state of the art still image compression methods the

major information loss is at the boundaries, applying ISMP compression which actually preserves the boundary or edge information, provides unparalleled fundamental compression ratio/PSNR trade off.

"Catastrophe" or alternatively isomorphic singular manifold as used ^{here} in this patent designates a mathematical object that describes the shape of 3-D object boundaries in *polynomial* form. The use of "catastrophe" theory for compression makes the present invention unlike all other compression methods because it helps to transmit information about 3-D object boundaries without loss, preserving the features of the object most valuable to human cognition, but with very high compression rate. By applying the present invention to still image compression, a 300:1 still image compression ratio with practically invisible artifacts (PSNR equal 32 dB) and a 4,000:1 full motion image compression ratio with fully developed natural motion and good image quality, is obtained.

The still image compression and related video compression technique of the present invention is extremely beneficial because, unlike other state of the art compression techniques, major information losses do not occur from compression at 3-D object boundaries (edges) that require both high dynamic range and high resolution (i.e., both high spatial and high vertical: "Lebesque" resolution). In these edges there is a vast amount of information necessary for many processing operations vital to a quality image and human cognition. The compression technique of the present invention, unlike other compression methods, preserves intact all "soft-"edge information without data loss. Hence, the present inventors have coined the term lossless-on-the-edges (LOTE)

compression. LOTE compression is possible because of the fully isomorphic projection between the 3-D object boundary vicinity and its 2-D projection on the screen. This fully isomorphic projection between the 3-D object boundary and the 2-D projection is based on Arnold's so called "catastrophe" theory that has been adapted to still image compression here. The methodology of the present invention works especially well with objects that are closer to sculptures and objects that have mostly flat surfaces combined with edgy features, i.e., very low or high spatial frequencies. This is exactly the opposite of Fourier analysis which does not work well with very low or very high frequencies. For low frequency, Fourier analysis is unsatisfactory because the coefficients must be very well balanced and at the same time can easily be hidden in noise. For high frequency components of objects such as edges, many high frequency components exist which Fourier methods eliminate. These high frequency components are what make up all important edges of the object and eliminating them reduces human cognition. ISMP analysis on the other hand, does not have this problem because it characterizes edges and objects using manifolds and hence preserves the information that makes up those edges and that was eliminated in Fourier-based compression methods.

Specific Features of the Human Perception of Visual Information and Object Recognition

An understanding of how humans recognize objects will make manifest the advantage of preserving information. The retina of the human eye contains millions of receptor cells, arranged in a mosaic-like pattern in the retinal layer. The receptor cells are cones and rods. These cones and rods provide the starting point for two separate but

without rather to detect and
rs. The visual system
images, faithfully reco
David Hubel and Tho

[illegible]

Human brain zones, which decode specific properties of image recognition, are spatially organized in the brain according to their function. Thus, different localized sets of neurons in the visual cortex are specialized to carry codes for contours, color, spatial position and movement. This segregation of functions explains why a person who has had a stroke, which damaged part of the cortex, sometimes loses the ability to see contours without losing the ability to see colors.

Special mechanisms of object edge extraction in the human visual system allow extraction of important objects from a background, even if the object has bulk colors very close to the colors of the second plane. The latter feature is extremely important for registration of military targets, and makes ISMP an effective compression algorithm
5 for ATR.

This still image compression performance can be transformed into analogous video image compression through the typical 10:1 factor for state of the art video image compression. Therefore, the inventive technique can be applied not only to high resolution digital video/still image transmission, but also to multi-media presentation,
10 high quality video conferencing, video servers, and the storage of large amounts of video information.

Catastrophe Theory Applied to Video Compression

Video compression is a four dimensional (4-D) problem where the goal is to remove spatial and temporal redundancy from the stream of video information. In video
15 there are scenes containing an object that continuously changes without jumps and has no edges, and, on the other hand, there are also scenes where there are cuts which are big jumps in the temporal domain or big jumps in the spatial domain (such as "edges"). These abrupt changes or jumps can be described as "catastrophes." Using catastrophe theory, these behaviors can be described by one or more elemental catastrophes. Each
20 of these elemental catastrophes describes a particular type of abrupt change in the temporal or spatial domains. In general, categorizing catastrophes in 4-D space is even

less established than catastrophe theory in general which is relatively unknown. Furthermore, 4-D space is far less understood than 3-D space but, similarities between them can be expected and can use projection-type mapping can be used, but in temporal space. One solution is to use spatial catastrophes along with temporal catastrophes.

- 5 In order to apply catastrophic theory to video imagery, a fourth "geometrical" coordinate, time, leading to time-space (4-D) is preferably added. In the case of the inventive isomorphic singular manifold projection (ISMP) methodology, five-dimensional (5-D) geometro-physical space (x, y, z, t, B) , where B is brightness, or luminance, is obtained. This 4-D time-space (x, y, z, t) plus physical coordinate, B , can be split into
- 10 4-D geometro-physical space, and time (t) and treated separately except in the case of relativistic velocities. In the latter, relativistic case, the 5-D space can be analyzed by Poincare group formalism. In the common, non-relativistic case, however, temporal singularities (catastrophic) may be described in the time-luminance (t, B) domain only. The time-luminance singularities may interfere with spatial singularities (previously
- 15 discussed). In such a mode of operation, each block of the image is represented by a single time-variable value.

- According to Figure 8, there are only two possible singularities describing any type of mapping including smooth curve projection designated (1) shown in Figure 8 where $\langle B \rangle$ is the average B -value characterizing a frame as a total structure (the
- 20 smooth projection shown in Figure 8 represents movement of a physical object. Item (2) in Figure 8 representing a catastrophic frame change, and item (3) representing position/tilt/zoom camera changes. The critical $\langle B \rangle$ -parameter may be, for example,

an average block-to-block error (e.g. mean square error). In summary, temporal catastrophic formalisms can be applied to MPEG hypercompression by replacing the average error parameters by integrated luminance-changes.

Canonical Polynomials

5 One way to represent these 4-D catastrophes is to use well known 3-D projections or mapping catastrophes which were discovered in the early 1980's. These "transformations" or "reconstructions" or "metamorphoses" in time are 4-D problems which can be separated into two 3-D problems: 1) Spatial catastrophes may be defined in 3-D space (x, y, B) such as occurs when there is a large change in intensity, B, over
 10 a small change in x, y; ^{2) temporal} ~~2) Temporal~~ catastrophes may also be defined temporally such as occurs where there is an abrupt change in motion over time such as is present during the rotation of an object or a cut from one scene to another. The 3-D temporal problem can be further reduced to a 2-D problem by transferring the (x, y, B) coordinates into 1-D merit space. Merit space is defined by the lack of similarity between frames in
 15 time.

Images are 3-D distributions of intensity. Abrupt changes in intensity occurring over small changes in x, y may be treated as catastrophic changes. The inventors have modified catastrophe theory to fit images and to solve the problems of image and video compression. The inventors have introduced a physical coordinate, B (luminance) into
 20 conventional geometrical coordinates to create "geometro-physical" surfaces.

There exists a finite list of fourteen polynomials or "germs" which describe different edge transitions or projections in mapping in 3-D space. Typically, only about three of these polynomials or germs are necessary to describe virtually every edge effect. The others are used on occasion to describe spatial projections.

- 5 The germs of the projections are equivalent to the germs of the projections of the surfaces $z = f(x,y)$ along the x-axis. The table below identifies the fourteen polynomials or germs.

Type	$f(x,y)$	Type	$f(x,y)$
1	x (without singularities)	8	$x^4 + x^2y + xy^2$
2	x^2 (fold)	9, 10	$x^5 \pm x^3y + xy$
3	$x^3 + xy$ (Whitney's tuck)	11,12	$x^3 \pm xy^4$
4, 5	$x^3 \pm xy^2$ (3/1 type curve)	13	$x^4 + x^2y + xy^3$
6	$x^3 + xy^3$ (9/2 type curve)	14	$x^5 + xy$
7	$x^4 + xy$ (4/3 type curve)		

In theory, a projection of a surface does not have any germs that are inequivalent to the fourteen germs in the above table. It should be understood that the Spectral Series for Reduction to the Normal Form (SSRNF) method is used for the unique reduction of the arbitrary polynomial to the germs presented in the above table. It is presented here only

- 5 in a descriptive form:

Let e_1, \dots, e_n - quasihomogeneous polynomial ($N+p$ degree) that generates

$$A_p^{\tau+1}$$

for diffeomorphism.

Then, there is formal diffeomorphism

•
•
•

The following is an abbreviated description of the still image compression method as in the flow chart of Figure 9. Step 1 involves segmenting the original image into

blocks of pixels, for example 16 x 16. Step 2 is to create a model surface for each segment or block corresponding to the original image so that there is isomorphism between the original image and the polynomial surface in accordance with Arnold's Theorem. More particularly this may involve calculating the equation F_{modelled} for each block or segment by substituting for variables in canonical polynomials. (See Steps 3-7 of detailed flow chart which follows). This step inherently eliminates texture of the image and emphasizes the "sculpture" characteristics. Step 3 is to optimize each model segment. This is done by calculating the difference between the original and model segments and choosing coefficients for the canonical polynomial which have the lowest Q i.e., the smallest amount of difference between the original segment and the modelled segment. This is repeated on a segment by segment basis. (See Steps 8-12 of the detailed flow chart which follows). Step 4 is to find connections between adjacent segments to create an entire image i.e., a model image of the entire frame. (See Steps 14-18 of the detailed flow chart). This yields an entire image that has only the "sculpture" characteristics of the original image and eliminates texture. Step 5 is to calculate the peak signal to noise ratio PSNR over the entire image and where the PSNR of the entire image is less than a threshold, the difference between the original image and the modelled image is calculated. This step recreates the texture information of the original image that was lost during the process. Thus, after this step there are two sets of data: the "sculpture" characteristics represented by a few discrete numbers or "datery" and the texture information of the image. (See Steps 19-21) Step 6 is to use standard lossy compression on the texture portion of the data and then to combine the texture and

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datery and apply standard lossless compression to that combined data. (See Steps 22-24 of the detailed flow chart).

Now the preferred still image encoding method will be described in detail in relation to the detailed flow chart.

5 In the following description of the still image encoding process according to the present invention the following definitions are used:

I_o = original I frame

I_m = modeled I frame

I_d = difference I frame ($I_d = I_o - I_m$ for each frame)

10 i_o = segment or block of original frame

i_m = segment or block of modeled frame

i_d = segment or block of difference frame ($i_d = i_o - i_m$ for each block)

Referring now to Figure 10, this figure sets forth a flow chart of the still image encoding process according to the present invention. In step 1, the next still image or I_o frame is captured. If only still images are being compressed for still image purposes, this image will represent one of those still images. If video is being compressed, the still image to be compressed here is one of the video's I frames which will be compressed in accordance with this method and then inserted at the appropriate location into the video bitstream.

20 In step 2, the original image I_o is segmented into blocks of pixels of any desired size such as, for example, 16 x 16 square blocks. The original image is seen in Fig. 11A. Any segment size may be used as desired. These segments or blocks of pixels are

As an example, the total number of segments or blocks for a 512 x 512 image is $512 \times 512 / (16 \times 16) = 1024$ different noninterleaving 16 x 16 segments or blocks.

5

$$R = \max(i_o) - \min(i_o)$$

10

15

Turning now to **step 5**, a first canonical polynomial from the table is taken. In **step 6**, substitutions for variables in the canonical polynomials are found. It is possible

to apply (1) a nonhomogeneous linear transformation (shift of coordinates), (2) a homogeneous linear transformation (rotation of axis) or (3) a nonhomogeneous nonlinear transformation. For example, if the canonical polynomial

$$f_{\text{canonical}} = x_1^3 + x_1 x_2$$

is taken from the table, variables x_1 and x_2 are substituted for as follows using the third example above nonhomogeneous nonlinear transformation:

$$x_1 = (y_1 + a_1 y_1^2 + \dots a_n y_n^2); x_2 = (y_2 + b_1 y_2^2 + \dots b_n y_n^2).$$

From this substitution a function describing a "modeled" surface (as opposed to the original image surface) is generated as follows:

$$\begin{aligned} f_{\text{model}} &= (y_1^2 + a^2 y_1^4 + 2a y_1^3)(y_1 + a y_1^2) + y_1 y_2 + a b y_1 y_2^2 + a y_1 y_2 + b y_1 y_2^2 \\ &= y_1^3 + a^2 y_1^5 + 2a y_1^4 + a y_1^4 + a^3 y_1^6 + 2a^2 y_1^5 + y_1 y_2 + a b y_1 y_2^2 + a y_1 y_2 + b y_1 y_2^2 \\ &= (y_1 + a y_1^2)^3 + (y_1 + a y_1^2)(y_2 + b y_2^2) \end{aligned}$$

At step 7, the modeled surface is created by substituting the coordinates of each pixel in the original segment or block into the equation f_{model} . A modelled surface is seen in Figure 11C. This creates a matrix containing the values $f_{m(1,1)}, x_{m(1,2)}, \dots$ as seen in Figure 12. Specifically, this matrix is created by substituting the coordinate of the pixel 1,1 from the original segment into the equation f_{model} to generate the element $f_{m(1,1)}$ in the modeled matrix. Next, the coordinate of the pixel 1,2 from the original segment is substituted into the equation f_{model} to generate value $f_{m(1,2)}$ which goes in the 1,2 pixel

location of the modeled surface. This is done for each pixel position of the original segment to create a corresponding modeled matrix using the equation f_{model} .

At step 8, Q is calculated by determining the difference between the original and modeled segments, pixel by pixel, using the equation:

$$Q = \sqrt{\frac{1}{MN} \sum_{x=0}^{M-1} \sum_{y=0}^{N-1} (i_o(x,y) - i_m(x,y))^2}$$

- 5 In other words, Q is calculated by subtracting corresponding pixels from the i_o segment (the original segment) from the i_m (the modeled segment) and squaring this subtraction and summing up all these squares.

- At step 9, Q is compared to a predetermined threshold Q_o based on image quality desired. Q should be less than Q_o because the point of the step 8 is to minimize the sum of the differences between the analogous pixels in the original and modeled frames so as to generate a modeled surface that is as close as possible to the original surface. If Q is greater than Q_o , the procedure loops back up to step 6 where new coefficients are tried in the same polynomial. Then steps 7, 8, and 9 are repeated, and if Q is less than Q_o with that new set of coefficients, then the process continues into step 10 where that Q and the coefficients that produced the lowest Q for that polynomial are stored. After storage at step 10, the process loops back up to step 5 if all polynomials have not yet been tested where the next canonical polynomial from the library is chosen and tested and solved for coefficients which produce the lowest Q for that next polynomial. Hence, steps 6, 7, 8, and 9 are repeated for that next polynomial until coefficients are found which produce the lowest Q for that polynomial. At step 10, the Q and the coefficients

for that next polynomial are stored. This process of steps 5, 6, 7, 8, 9, and 10 is repeated for each polynomial in the library. After each polynomial in the library is tested for the segment under test, the process moves to step 11.

At step 11, the polynomial having the lowest Q of the polynomials tested for that segment is chosen. That polynomial is transferred to step 12.

At step 12, all coefficients for the chosen polynomial (the one having the lowest Q of all the polynomials tested for that segment) are stored. These coefficients are coefficients of the equation f_{model} which describes the modeled surface.

After step 12, the next set of operations involves segment by segment operation working only with the polynomials and their coefficients whereas the above steps 5-12 worked with the matrix representation of each segment. Because only the polynomials and their coefficients are worked with in the next set of operations, a significant amount of compression has taken place because the data representing the surface is far less voluminous than when a matrix representation of the segments is worked with. The data is simply coefficients of polynomials which can be called "datery".

At step 13, the current segment is taken or captured from the above steps. At step 14, a connection is found between adjacent or neighboring segments by extending the surface of a first segment into a second segment and finding differences between the extended surface and the second segment surface. Specifically, this is done by finding the average distance "q" between the surface which extends from the first segment into the second segment and the surface of the second segment using standard methods. If the average distance "q" is smaller than a threshold value q_0 , the surface of the second

segment is approximated by the extended surface. In other words, if the distance q is smaller than the threshold value q_0 , the second segment surface is thrown out because it can be approximated satisfactorily by substituting the extended surface in its place. If the average distance q is greater than the threshold value q_0 , a connection needs to be found between the extended surface and the surface of the second segment.

Thus, at step 15, the average distance q is checked to determine whether it is less than the threshold value q_0 . If it is, then the connections between the adjacent or neighboring segments which can be plotted as a graph, as seen in Figure 13, are stored on a segment by segment basis. In other words, as seen in Figure 13, the surfaces which extend from, say, a surface in segment "9" into adjacent or neighboring segments (8, 10, 14 and 15), if any, are stored in the polynomial for segment 9 (earlier calculated and then stored at step 12) which then represents that graph of connections between segment 9 and segment 8, 10, 14 and 15. In other words, the polynomial that was calculated and stored for the segment in question, here segment 9, is modified so that it now extends into adjacent segments 8, 10, 14, and 15 and represents the surfaces in those segments. The polynomials for segments 8, 9, 10, 14 will be substituted with the new bigger scale polynomial obtained from 9.

If the average distance from 9 was not less than q_0 (which indicates that the surface extended from the segment in question, segment 9 for example, into an adjacent segment, 8, 10, 14, or 15 for example, did not satisfactorily approximate the surface of the second segment), then a spline must be calculated at step 17.

At step 17 splines are calculated from the segment with adjacent segments using standard spline equations which need not be detailed here.

After both steps 16 and 17, the process continues at step 18. At step 18, a model image i_m is created of the entire frame by creating a table of all segments for that frame using the information calculated for each segment in the above steps. The creation of this table representing the entire frame from its numerous segments is analogous to step 7 where a modeled segment was created by substituting the pixel coordinates from the original segment into the f_{model} polynomial to get a matrix describing the modeled surface. At step 18, however, instead of creating a modeled segment of pixels, a modeled frame is created from modeled segments. Thus, it can be seen that the smaller parts calculated above are now being combined to generate an entire modeled frame.

After step 19, the peak signal to noise ratio (PSNR) is calculated over the entire image using the equation:

$$PSNR = \frac{10 \log_{10} (\text{number of gray scale levels})^2}{Q}$$

$$Q = \sqrt{\frac{1}{hv} \sum_{x=0}^{M-1} \sum_{y=0}^{N-1} [I_o(x,y) - I_m(x,y)]^2}$$

h and v are number of pixels in horizontal and vertical directions respectively for the entire frame image. The Q values for each of the segments were stored at step 10 above and may be retrieved for this purpose.

5 compress the frame data. The compressed data is then sent to storage or a
communication link.

10 pixels in I_0 and a new frame I_d is created (see Figure 14) where each pixel in that frame has as its value the difference between the corresponding pixels in the frame I_0 and the frame I_m . The frame I_d therefore corresponds to the high frequency components, such as edge information which typically is lost in conventional compression techniques. This "texture" information containing high frequency components and edge information is then

15 compressed separately at step 22.

20 frame is stored. This concludes the compression of the still frame or I_0 frame.

As can be seen, the polynomial surface image is highly compressed because it is stored and transmitted as a complex algorithm (polynomial) rather than as a matrix

representation. Additionally, the edge contour image I_d is separated from the polynomial surface, as a by-product of characterizing the original image by a canonical polynomial and contains the high frequency and edge components and is itself compressed.

Preferred Still Image Decoding Method

5 The still image decoding process will now be described as seen in the flow chart of Figure 15. The input to the still image decoding process will be either just the whole frame I_m in the case where the PSNR of the whole frame at step 20 was not less than threshold P_0 or the whole frame I_m plus I_d' where the PSNR of the whole frame at step 20 was less than P_0 and the differences between the original I_0 frame and the modeled frame I_m were calculated to create new frame I_d holding the textured or high frequency and edge information.

10 In either case, the first step in decoding is step 1 which decodes the lossless compression data from the encoder which was compressed at step 24. At step 2 of the decoding process, frame I_m is separated from the other data in the bitstream. At step 3, the first graph or segment which was stored at step 16 on a segment by segment basis is taken.

15 At step 4, whether the segment belongs to a graph (i.e., has connections to adjacent segments) or is an isolated segment (i.e., has no connections to neighboring segments) is tested. If the segment does belong to a graph, then at step 5, a segment i_m is constructed for each graph (analogous to the creation of the modeled matrix

20

surface in step 7 of the encoding process) using the polynomial that was stored for that graph at step 16 of the encoding process.

If the segment does not belong to a graph, then after step 4 the process skips step 5 and continues with step 6.

5 At step 6, the separate graphs using standard splines are connected. In other words, those segments from steps 14, 15, and 17 which were connected by splines will be reconnected here. (Recall that it was these segments for which the extended surface of another adjacent segment did not satisfactorily characterize the surface of these segments and therefore a spline equation had to be used.)

10 From step 5 where a segment i_m for each graph was reconstructed, and from step 6 where separate graphs were connected using standard splines, the process continues at step 7.

At step 7, the frame I_m is constructed using segments from step 5 (in the same way as the frame I_m was constructed in the encoding process at step 18 and also
15 similar to how an individual segment or modeled surface or modeled segment was created at step 7 in the encoding process.)

At step 8, the presence of a I_d' frame for or in conjunction with the frame I_m is tested. If there is no frame I_d' , then the process is finished and the still image is fully decoded for that frame. If on the other hand there is a frame I_d' in conjunction with
20 the frame i_m , then the process continues to step 9.

At step 9, the frame I_d' is decompressed.

At step 10, frame I_0' is created from the combination of frame I_m from step 7 of the decoding process and frame I_d' from step 9 of the decoding process. After the frame I_0' is created, the process is finished and the still image is fully decoded.

Preferred Video Compression Method -- Motion Estimation

5 The inventive compression technique for still images can be incorporated into standard MPEG compression to enhance video compression through spatial hypercompression of each I frame inserted into the video bitstream. Alternatively, in the preferred embodiment, a novel motion estimation technique is employed which provides significantly greater compression due to temporal compression. According to the present invention, I frames are inserted according to video content. This is done by accumulating the error or difference between all corresponding microblocks or segments of the current frame and the predicted frame and comparing that accumulated error or difference to a threshold to determine whether the next subsequent frame sent should be an I frame. If the error or difference is large (i.e., when motion error is high), the I frame is sent. If the error or difference is small, the I frame is not sent and the frame sequence is unaltered. As a consequence, full synchronization of I frame insertion with changes in scene is achieved and bandwidth is significantly reduced because I frames are inserted only where necessary, i.e., where content requires them. Thus, the present invention, for the first time, analyzes the errors between the I frame and the B and P frames into which it will be inserted to decide whether to insert the I frame at that point or not. Consequently, the present

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invention significantly increases the overall image compression ratio, while offering a simultaneous benefit of increased image quality. In addition, by using the technique of the present invention for video compression, the distances between I frames are enlarged, which leads to better motion estimation and prediction.

- 5 The video compression technique of the present invention may be used with both I frames compressed using the still ISMP compression encoding process of the present invention or standard I frame compression techniques. The most significant compression will occur if both the ISMP compression encoding process of the present invention and the motion estimation process of the present invention are used. It is
- 10 worth noting that in existing systems, a reasonable quality video can be produced only if I frame compression is not higher than 20:1 to 40:1. With the present invention I frame compression of 300:1 is achieved. The following table illustrates the improvement over standard compression of the inventive technique of fixed separation of I frames compressed with the inventive CT algorithm used in conjunction with the
- 15 inventive variable separation of I frames compressed with the CT algorithm.

	Standard Compression	Fixed separation with I frames compressed with CT algorithm	Variable separation of I frames compressed with CT algorithm
Image Resolution (8-bit per pixel)	352 x 240	352 x 240	352 x 240
Uncompressed Image Size per Frame	84,480	84,480	84,480
I Frame Compression	30:1	300:1	100:1

Motion estimation is important to compression because many frames in full motion video are temporally correlated, e.g., a moving object on a solid background such as an image of a moving car will have high similarity from frame to frame. Efficient compression can be achieved if each component or block of the current frame to be encoded is represented by its difference with the most similar component, called the predictor, in the previous frame and by a vector expressing the relative position of the two blocks from the current frame to the predicted frame. The original block can be reconstructed from the difference, the motion vector, and the previous frame. The frame to be compensated can be partitioned into microblocks which are processed individually. In a current frame, microblocks of pixels, for example 8×8 , are selected and the search for the closest match in the previous frame is performed. As a criterion of the best match, the mean absolute error is the most

Efficient compression can be achieved if each component or block of the current frame to be encoded is represented by its difference with the most similar component, called the predictor, in the previous frame and by a vector expressing the relative position of the two blocks from the current frame to the predicted frame. The original block can be reconstructed from the difference, the motion vector, and the previous frame. The frame to be compensated can be partitioned into microblocks which are processed individually. In a current frame, microblocks of pixels, for example 8×8 , are selected and the search for the closest match in the previous frame is performed. As a criterion of the best match, the mean absolute error is the most

often used because of the good trade off between complexity and efficiency. The search for a match in the previous frame is performed in a, for example, 16×16 pixels window for an 8×8 reference or microblock. A total of, for example, 81 candidate blocks may be compared for the closest match. Larger search windows are possible using larger blocks 8×32 or 16×16 where the search window is 15 pixels larger in each direction leading to 256 candidate blocks and as many motion vectors to be compared for the closest match.

Once the third subsequent frame is predicted, the standard methods provide that the error between a microblock in the current frame and the corresponding microblock in the predicted frame are compared and the error or difference between them is determined. This is done on a microblock by microblock basis until all microblocks in the current frame are compared to all the microblocks in the predicted frame. In the standard process these differences are sent to the decoder real time to be used by the decoder to reconstruct the original block from the difference, the motion vector, and the previous frame. The error information is not used in any other way.

In contrast, in the present invention, the error or difference calculated between microblocks in the current frame and the predicted frame are accumulated or stored and each time an error is calculated between a microblock in the current frame and the corresponding microblock in the predicted frame that error is accumulated to the existing error for that frame. Once all the errors for all the blocks in the current frame as compared to the predicted frame are generated and summed, that

accumulated error is then used to determine whether a new I frame should be inserted. This methodology is MPEG compatible and yields extremely high quality video images not possible with state of the art motion estimators. The accumulated error is used to advantage by comparing it to a threshold E_0 which is preset depending upon the content or type of the video such as action, documentary, or nature. If E_0 for a particular current frame is exceeded by the accumulated error, this means that there is a significant change in the scene which warrants sending an entire new I frame. Consequently, an entire new I frame is compressed and sent, and the motion estimation sequence begins again with that new I frame. If E_0 is not exceeded by the accumulated error, then the differences between the current frame and the predicted frame are sent as usual and this process continues until E_0 is exceeded and the motion estimation sequence is begun again with the sending of a new I frame.

Now turning to Figure 16, the motion estimation process is now described in detail. At step 1, the next F_0 frame is taken. This frame may be the first frame of the video in which case it is an I frame or may be a subsequent frame. At step 2, if F_0 was compressed by standard DCT methods, the left branch of the flow chart of Figure 8 is followed. If F_0 was compressed using the inventive ISMP algorithm, the right branch of the flow chart in Figure 8 is followed.

First, assuming that F_0 was compressed using standard DCT methods, step 3 involves standard segmenting of the F_0 frame into search blocks having subblocks called microblocks and defining motion vectors which are used to predict the third

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subsequent frame after F_0 . This is accomplished using standard techniques well known in the art.

At step 4, the error or difference between each microblock in F_0 and the corresponding microblock in the predicted third subsequent frame is defined for all microblocks in F_0 . At this point the inventive motion estimation process ~~process~~ diverges from standard techniques.

If a standard MPEG encoder-decoder scheme was being used, these microblock differences would be sent from the encoder to the decoder and used by the decoder to reconstruct F_0 . By sending only the differences between F_0 and the predicted third subsequent frame, significant compression is realized because it is no longer necessary to send an entire frame of information but only the differences between them. In accordance with standard MPEG encoder-decoder techniques, however, a new I frame is necessarily transmitted every 15 frames whether an I frame is needed or not. This poses two problems. Where the I frame is not needed, bandwidth is wasted because unnecessary bits are sent from the encoder to the decoder (or stored on disc if the process is not done real time). On the other hand, where the content of the video is such that significant scene changes occur from one frame to another much more often than every 15 frames, the insertion of an I frame every 15 frames will be insufficient to ensure a high quality video image at the decoder. For these reasons, the motion estimation technique of the present invention is especially valuable because it will, dependent upon the content of the video, insert

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predicted 3rd subsequent frame?

or send an I frame to the decoder when the content of the video warrants it. In this way, a high quality image is maintained.

This is accomplished in the present invention by, as seen at step 5, accumulating the error between corresponding microblocks in the F_0 and the predicted third subsequent frame as each error is defined in step 4 for each microblock of F_0 .

The next step, step 6, is optional and involves normalizing the total accumulated error for F_0 by defining an average error A which is the total accumulated error divided by the number of microblocks in F_0 . This yields a smaller dynamic range for the errors; i.e., smaller numbers may represent the errors.

Continuing with step 7, the accumulated error (whether normalized or not) is compared to a threshold error E_0 . E_0 is chosen based upon video content such as whether the video is an action film, a documentary, a nature film, or other. Action videos tend to require insertion of I frames more often because there are more drastic changes in scene from one frame to another. It is especially important when compressing such videos to use the motion estimation technique of the present invention which can insert additional I frames based on video content where necessary to keep video image quality high. In choosing E_0 , bandwidth versus quality should be considered. If E_0 is set high, a high level of errors will be tolerated and fewer I frames will need to be inserted. Quality, however, will decrease because there will be an under utilization of bandwidth. If, on the other hand, E_0 is set too low, I frames will be inserted more frequently and available bandwidth may be exceeded and frames may start to drop out as commonly happens with MPEG. So the threshold E_0

should be tuned to video content. This can be done in real time by analyzing the video off-line and varying E_0 in accordance with the statistics of the video, such as the number of cuts, the amount of action, etc. This process may be enhanced by using genetic algorithms and fuzzy logic. Where the accumulated error is greater

- 5 than E_0 , the next frame sent will be an I frame. In accordance with standard techniques, it is preferable that the I frame be compressed prior to sending it to the decoder. This reinitiates the sequence of frames at step 8.

If the accumulated error is less than E_0 , the subsequent frame is not sent as an I frame but the differences are continued to be sent at step 9 to minimize bandwidth
10 of the signal, sent between the encoder and decoder. The process then reinitiates at step 1 where the next frame F_1 is taken. That next frame may not be an I frame but may instead be a subsequent frame, and the methodology is the same in either case. The next frame, whether it is an I, B, or P frame, is compared to the predicted third subsequent frame and the method continues as described above.

In an alternative embodiment, instead of sending the I frame as the next subsequent frame, the I frame could be sent as the current frame and used to replace error data for each microblock data for each microblock stored in the decoder buffers. This could be accomplished by clearing the buffers in the decoder holding errors between each of the microblocks F_0 and the predicted third subsequent frame and replacing that data with the I frame. Although not compatible with MPEG, it may be advantageous in certain situations to clear out the buffers containing the high error frame data and replace that data with the next frame as an I frame.

15
This seems to suggest differences in sent (large) bit error is big event? then the next frame is sent
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whole (I-frame)
b/c b/c → send
that don't send bits.
if 100 bits send 2 frame
0 66-67

This is compared

The motion estimation technique of the present invention may also be used to dynamically change or update compression ratio on a frame by frame basis by providing feedback from the receiver or decoder and using that feedback to change parameters of the compression engine in the registers of the video compression chips.

5 For example, if the accumulated error calculated in the motion estimation technique of the present invention were too frequent or extraordinarily high, this information could be used to alter the parameters of the compression engine in the video compression chips to decrease the compression ratio and thereby increase bandwidth. Conversely, if the accumulated error over time was found to be unusually low, the compression
10 ratio could be increased and thereby the bandwidth of the signal to be stored could be decreased. This is made possible by the accumulation of errors between the corresponding microblocks of the current frame (F_0) and the predicted third subsequent frame. This is not possible in prior art techniques because, although the error between corresponding microblocks of the current frame and the predicted third
15 subsequent frame are calculated, there is no accumulated error calculated and no use of that accumulated error anywhere in the system. In the present invention, however, the accumulated error is calculated and may, in fact, be used on a frame by frame basis to decide whether the next frame should be an entire I frame as opposed to only the difference signal.

20 In a bandwidth on demand system, for example, if the feedback from the receiver indicates that there is a high bit error rate (BER), the transmitter may lower the bandwidth by increasing the compression ratio. This will necessarily result in a

signal having sequences of different bit rates which are not possible in prior art MPEG systems. Intelligent systems such as genetic algorithms or neural networks and fuzzy logic may be used to determine the necessary change in compression ratio and bandwidth off-line by analyzing the video frame by frame.

5 Turning now to the right branch of Figure 16, this branch is followed if the still compression method selected was the ISMP algorithm of the present invention which compresses each frame in accordance with catastrophic theory and represents the "structure" of that image in a highly compressible form using only the coefficients of canonical polynomials. Step 3A in the right branch would be to predict the third
10 subsequent frame from the current frame (here F_0) using standard techniques of defining the motion vectors of microblocks within the search blocks by template matching.

 Step 4A would be to define the error between microblocks in F_0 and the microblocks in the predicted third subsequent frame. This is done using standard
15 techniques. If a particular microblock in F_0 has a match with a microblock in the predicted frame, i.e., the error is 0, then the coefficients of the polynomial that were generated for that microblock when F_0 was compressed using the ISMP algorithm are then sent to the decoder and used along with the motion vectors generated in step 3A to reconstruct F_0 . The sending of just the coefficients results in much higher than
20 normal compression because the number of bits representing those coefficients is very small. If a microblock in F_0 has no match in the predicted third subsequent frame i.e., an error exists between those corresponding microblocks, new coefficients are

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generated for the corresponding microblock in the predicted third subsequent frame and those coefficients are sent to the decoder and used along with the motion vectors generated in step 3A to reconstruct F_0 . As an alternative, the newly generated coefficients for the corresponding microblock in the predicted third subsequent frame could be subtracted from the coefficients of the corresponding microblock in F_0 to even further compress the data. This may be done but is not necessary because the coefficients representing each microblock constitute highly compressed data already and further compression is not necessary.

At step 5A, the errors from the above comparison of F_0 and P are accumulated.

At step 6A, the accumulated errors are normalized by the number of microblocks.

At step 7A, the accumulated error is compared to the threshold E_0 . And if the accumulated error is greater than the threshold E_0 a new I frame is sent as the new subsequent frame at step 8A. If the accumulated error is less than the threshold error E_0 the coefficients that were newly generated for a particular microblock that did not find a match are continued to be sent to the decoder at step 9A. After both steps 8A and 9A the process reinitiates at step 1. Thus, according to the present invention, the error data is used and interpreted in a novel way which provides high compression and quality imaging.

Motion Estimation Hardware

Referring now to Figure 17, the hardware for performing motion estimation is depicted in block diagram format. All of the hardware is standard. A host computer 10 communicates with video processor board 12 over PCI bus 14. The host computer 10 is preferably of at least the 100 MHz ^{the} Pentium class. PCI bus controller 12 controls communications over the PCI bus. EPROM 14 stores the coefficients and transfers them to the PCI bus controller 12 so that all the internal registers of the PCI bus controller 12 are set upon start-up. Input video processor 16 is a standard input video processor. It is responsible for scaling and dropping pixels from a frame. It has two inputs, a standard composite NTS signal and a high resolution Y/C signal having separated luminance and chromance signals to prevent contamination. The input video processor 16 scales the normal 702 x 480 resolution of the NTS input to standard MPEG-1 resolution of 352 x 240. The input video processor 16 also contains an A/D converter which converts the input signals from analog to a digital output. ^(not shown)

Below input video processor 16 is audio input processor 18 which has as its input left and right stereo signals. The audio input processor 18 performs A/D conversion of the input signals. The output of the audio input processor 18 is input to a digital signal processor (DSP) audio compression chip 20 which is standard. The output of the audio compression chip 20 is input into the PCI bus controller 12 which can place the compressed audio onto the PCI bus 14 for communication to the host computer 10. Returning to the video side, the output of the input video processor 16

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is input to an ASIC 22 (Application Specific Integrated Circuit) which is one chip of a three chip video compression processor ²³ also having a DTC based compression chip 24 and a motion estimator chip 26. The ASIC 22 handles signal transport, buffering and formatting of the video data from the input video processor 16 and also controls both

5 the DTC based compression chip 24 and motion estimator chip 26. All of these chips are standard. An output of each of the chips 22, 24, and 26 of the video compression processor ²³ is input to the PCI bus controller 12 for placing the compressed video on the PCI bus ¹⁴ for communication to the host computer 10.

The compressed video stream from the video compression processor 23 on the

10 board ¹³ undergoes lossless compression in the host computer using standard lossless compression techniques such as statistical encoding and run-length coding. After that lossless compression, the audio and video are multiplexed in standard fashion into a standard video signal. In order to have synchronization of audio and video the packets containing video and audio must be interleaved into a single bit stream with

15 proper labeling so that upon playback they can be reassembled as is well known in the art.

Importantly, the errors that were calculated in the motion estimator 26 between the current frame and the predicted third subsequent frame are transmitted to the host computer 10 over the PCI bus 14 so they can be transmitted to the encoder (not

20 shown) to recreate the current frame at the encoder using that error or difference signal and the motion vectors generated during motion estimation. This is standard in the art. In accordance with the motion estimation of the present invention, however,

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Figure 18 is a flow c
procedure. At Step 1 th
is shown

Referring now to Figure 18, ~~is~~ is a flow chart describing error accumulation in the motion estimation procedure. At Step 1 the error buffer in the compression processor 23 is read through the PCI bus 14. At Step 2 that error is accumulated in an error buffer created in software in the host computer 10 so that the accumulated error will equal the preexisting error plus the present error. At Step 3 the accumulated error is compared to a threshold error and if the accumulated error is larger than the threshold error then a new I frame is sent and the error buffer in the compression processor need not be read again for that particular frame. If the accumulated error is not greater than the threshold error then the process loops back up to Step 4 where the next subsequent microblock in that frame is chosen. If there is a subsequent microblock in that frame then the process repeats at Step 1 where the error buffer in the compression processor is read. That error is accumulated in the accumulated error buffer at Step 2 and that accumulated error is compared to threshold at Step 3. Note that this looping will continue from Steps 1, 2, 3, and 4 until at Step 3 the accumulated error exceeds the threshold at which point it is no longer necessary to check any more microblocks for that frame because the error became so high that the host computer determined that a new I frame should be sent to restart the motion sequence. If, on the other hand, the accumulated error for all the microblocks of an entire frame never exceeds the threshold, then after Step 4, the

process will go to Step 5 and the standard MPEG compression process will continue without changes, i.e., the next B or P frame will be grabbed and compressed.

Automatic Target Recognition (ATR)

5 The ISMP still image compression methodology of the present invention can be used to greatly enhance automatic target recognition systems because the invention emphasizes and accurately represents the natural features such as "sculpture" of the object that makes human cognition of the target easier and more accurate.

Furthermore, the polynomials used to represent the sculpture of the object are stable for small variations of projection direction or changes in movement, rotation, and
10 scale of an object. This, too, enhances automatic target recognition.

Human vision defines objects principally by their contours. The human visual system registers a greater difference in brightness between adjacent visual images that are registered, faithfully recording the actual physical difference in light intensity.

15 Researchers have shown that individual neurons in the visual cortex are highly sensitive to contours, responding best not to circular spots but rather to light or dark bars or edges. At it turns out, the fact that ISMP compression extracts exactly these edges and emphasizes the "sculpture" characteristic of the object makes it especially advantageous for use in ATR. By preserving object edges in the compressed information, the human visual system can extract important objects from a
20 background even if the object has bulk colors very close to the colors of other objects

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in the background. This feature is extremely important for registration of military targets.

In virtually all ATR applications, the structures to be identified have sculpture. Consequently, the sculpture portion of the image can be extracted using the inventive methodology to achieve compression ratios of at least 4:1. Unlike prior art methods based on linear methods and Fourier transforms like JPEG and wavelet, which destroy the very information which is essential for human cognition-soft edges, the present invention preserves those soft edges that exist in sculptures in virtually all structures to be identified. In contrast, the "texture" of an object is far less critical to human cognition. The present invention takes advantage of the distinction between sculpture and soft edges and texture by separating the sculpture characteristics of the object from the texture characteristics and utilizing only the sculpture information for ATR. An additional benefit of this methodology is that the sculpture information may be transmitted using relatively little bandwidth because it can be fully represented by polynomials whereas texture information requires greater bandwidth.

A preferred method of ATR involves separating the texture and sculpture portions of the image using the ISMP compression method, using standard soft ATR on the sculpture portion, and then using standard hard ATR methods on the entire image (both texture and sculpture). Another preferred method for ATR in accordance with the ^{present} invention is to split the texture and sculpture portions of the image using a portion of the ISMP compression method, using state of the art soft ATR methods on the sculpture part, and then using state of the art hard ATR methods on

the sculpture part. The

[illegible]

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ISMP compression method emphasizes the sculpture characteristics of the object, it enhances the ability to recognize the object imaged. Second, because the "sculpture" characteristics of the object are emphasized and represented using discrete numbers or coefficients from polynomials, the data sent is highly compressed which increases
5 bandwidth significantly.

Another application is as an autonomous movie director where standard ATR is used and that information is compressed using the present invention for sending those images from the cameras to the central station. Because of the large volume of information that can be generated in such a system, the images must be compressed
10 sufficiently so that they do not overwhelm the host computer. This is a real problem that is solved by the hypercompression of the present invention. These benefits apply to a wide range of systems including battlefield imaging systems and anti-terrorist recognition applications as well as full mapping capabilities.

Another significant advantage of the present invention is the ability to provide
15 sufficiently high compression ratios for providing TV-class transmission through traditional air communication channels which are 64 kbps or less. In fact, the invention can provide such a significant compression ratio improvement of more than an order of magnitude that, generally speaking, "video through audio" is made possible. In other words, the present invention makes it possible for battlefield
20 commanders and others to receive image information as opposed to raw data. And because the image information they receive is sent in the form of discrete numbers or coefficients of polynomials that relate to isomorphic singular manifolds in the object,

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the data are highly compressed. And although highly compressed, the data preserve full information about the objects 3-D boundaries or soft edges.

An example of a real-time remote engagement (RTRE) air scenario made possible because of the present invention includes providing an aviator who is
5 approaching his target (at sea, on the ground, or in the air) with a short TV-relay from an overflying military communications aircraft or satellites that upgrades the present target location at the last minute. This can prevent an aviator from losing track of a highly mobile target. This is made possible because the data are highly compressed and can be sent over low bandwidth air channels of 64 kbps or less and
10 because the information that is sent preserves edge information which makes it possible for the pilot to easily recognize his target.

Because the typical air communication channels are of low bandwidth, the ability to use all that bandwidth is critical. The present invention's ability to dynamically allocate bandwidth on demand permits the use of small fractions of
15 standard 64 kbps bandwidths for bursty compressed video/graphic image transmission. A typical air communications channel must accommodate signals of different types such as imagery, audio, sensory data, computer data and synch signals etc. The higher level protocols of the network will prioritize these different signals. Conservatively speaking, imagery is one of the lowest priority because in most cases
20 operations can continue without it. Therefore, imagery information typically is relegated to using only the bandwidth that is available and that available bandwidth changes with time. It is extremely useful to use the ISMP method of the present

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5 permit imagery data to be sent where otherwise it was not possible to do so.

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compression of object boundaries and still preserves high image quality.

Experimental results show that the ISMP methodology of the present invention in contrast to state of the art compression methods can achieve a compression ratio of 160:1 at PSNR = 38 Db with almost invisible artifacts whereas the prior art offers
5 only CR = 60:1 at a lower PSNR value of 26 Db. The difference in the image is significant.

Where far less than 64 kbps bandwidth channels are available, the hypercompression made possible by the present invention can permit continuity of images by "cartooning" which allows transmission of reduced real-time video-
10 conferencing even on an 8 kbps communications channel.

Referring now to Figure 19, Figure 19 shows five categories of data reduction as a fraction of the original, five reduced data rates, and five different outcomes of those data rates. Category A represents 100% of the original which is a data rate of 64 kbps. At this data rate, the original video may be sent. Category B represents a
15 data reduction as a fraction of the original 75% which is a 48 kbps data rate. The result of this transmission is that tiny details of the face or other structure are still recognizable and edges remain unchanged. Category C represents a data reduction of 50% as a fraction of the original which is a data rate of 32 kbps. The result of this transmission is that edges are hardened and there are smooth transitions for face
20 details. Category D represents a 25% data reduction as a fraction of the original which is a reduced data rate of 16 kbps. The result of this transmission is a heavily reduced texture and hard edges but it is still possible to recognize a human face.

Various modes of carrying out the invention are contemplated as being within the scope of the following claims particularly pointing out and distinctly claiming the subject matter which is regarded as the invention.